

Maximum Time: 2 Hours

Max marks: 30

Attempt all the questions

1. (a) Prove or disprove whether the relation R , defined in the set A of all polygons as $R = \{(P_1, P_2) : P_1 \text{ and } P_2 \text{ have same number of sides}\}$ is an equivalence relation on A . (2.5)
(b) Let $S = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$. Prove or disprove whether the relation R on $A = S \times S$ defined by $(a, b)R(c, d)$ if and only if $10a + b \leq 10c + d$, is a partial order relation. (2.5)
(c) Without constructing truth table, prove the following
1. $\neg p \rightarrow (q \rightarrow r) \equiv q \rightarrow (p \vee r)$
2. $((p \vee q) \wedge \neg(\neg p \wedge (\neg q \vee \neg r))) \vee (\neg p \wedge \neg q) \vee (\neg p \wedge \neg r)$ is a tautology (5)
2. (a) Using law of inference, prove that, $p \vee q, q \rightarrow r, p \rightarrow s, \neg s \Rightarrow r \wedge (p \vee q)$. (5)
(b) Using Inference theory of predicate logic show that "Everyone who knows JAVA will get a high paying job" and "someone in this class knows JAVA" will logically conclude "someone in this class will get high paying job". (5)
3. (a) Prove that $\sqrt{2}$ is irrational. (4)
(b) Consider the poset, $P = \{1, 2, 5, 6, 10, 60, 420\}$, where relation aRb is $a|b$ stands for a divides b .
1. Draw the Hasse diagram for the poset P .
2. Find the maximal and minimal elements of P .
3. Determine whether the poset, P is a Lattice, with proper justification. (6)

*****Best wishes*****