

NATIONAL INSTITUTE OF TECHNOLOGY, KURUKSHETRA
THEORY EXAMINATION
Question Paper

Month and year: **Dec. 2019**
Program: **B.Tech.-CS**
Subject: **DAA**
Maximum Marks: **50**
Number of Questions to be attempted: **5**

Total no. of pages used: **2**
Semester: **III**
Course code: **CSPC-21**
Time allowed: **03 Hours**
Total No of Questions: **5**

Note 1: Question No. 5 has an internal choice. Attempt any one part of it.

Note 2: Unless stated otherwise, the symbols have their usual meanings in context with subject. Assume suitably and state, additional data required, if any.

| | | |
|-------------|--|---|
| Q-1. | (a). Define Heap and analyze the complexity of min heap function. | 2 |
| | (b). Explain Prim's Algorithm for minimum Spanning tree. Also compute its time complexity. | 2 |
| | (c). Define B-Tree with its terminology. Also insert following in a B-Tree having order 3. 7, 3, 5, 11, 16, 4, 9, 2 | 2 |
| | (d). How backtracking algorithm solves the Hamiltonian problem? Explain. | 2 |
| | (e). Write pseudo code to find strongly connected component in a graph. | 2 |
| Q-2. | (a). Solve following recurrence relation using recursion tree method. $T(n) = \begin{cases} 1 & \text{if } n = 1 \\ T(n/3) + T(2n/3) + \theta(n) & \text{if } n > 1 \end{cases}$ | 3 |
| | (b). What is graph coloring problem? Write the pseudo code to color a graph and also analyze its complexity. | 3 |
| | (c). Write the pseudo code to solve 8-queen problem using the backtracking algorithm. Show all the steps of 4-queen problem and analyze the complexity of n-queen problem. | 4 |
| Q-3. | (a). Prove the master theorem. | 5 |
| | (b). Write the algorithms to solve the rod-cutting problem. Also analyze its time complexity. | 5 |
| Q-4. | (a) Define the elements of the Dynamic Programming. Write all the steps to find the LCS of two string X = <ABCDGH> and Y = <AEDFHR>. | 4 |
| | (b) Write the pseudo code for Johnson's algorithm. Professor Greenstreet claims that there is a simpler way to reweight edges than the method used in Johnson's algorithm. Letting $w^* = \min_{(u,v) \in E} \{w(u,v)\}$, just define $\hat{w}(u,v) = w(u,v) - w^*$ for all edges $(u,v) \in E$. what is wrong with the professor's method of reweighting? | 6 |

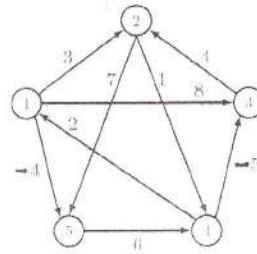
Q-5.

- (a) What is task scheduling problem? Find optimal sequence of Jobs for following jobs using greedy algorithm.

| Job | J_1 | J_2 | J_3 | J_4 | J_5 |
|----------|-------|-------|-------|-------|-------|
| Deadline | 2 | 1 | 3 | 2 | 1 |
| Profit | 60 | 100 | 20 | 40 | 20 |

- (b). Find the optimal parenthesis of matrix chain multiplication where sequence of dimensions is $A_1:10 \times 100$, $A_2:100 \times 5$, $A_3:5 \times 50$, $A_4:50 \times 20$

- (c) Explain Floyd-Warshall Algorithm to find all pair shortest path. Find all pair shortest path of following problem also analyze its complexity.



OR

- (a) What is priority queue? Illustrate the operation of HEAP-EXTRACT-MAX on the heap $A = \langle 15, 13, 9, 5, 12, 8, 7, 4, 0, 6, 2, 1 \rangle$.

- (b) Write the pseudo code for Huffman codes. Generate the Huffman code for following symbols.

| Symbol | a | b | c | d | e | f |
|-----------|---|----|---|---|----|---|
| Frequency | 6 | 11 | 9 | 2 | 20 | 5 |

- (c) Let $G=(V, E)$ be a weighted, directed graph with nonnegative weight function $w: E \rightarrow \{0, 1, \dots, W\}$ for some nonnegative integer W . Modify Dijkstra's algorithm to compute the shortest paths from a given source vertex s in $O(WV + E)$ time.