

**DEPARTMENT OF MATHEMATICS**  
**NATIONAL INSTITUTE OF TECHNOLOGY, KURUKSHETRA**

B.Tech. First Semester (CE, EE, EC, ME, PI)  
Differential Calculus and Differential Equations (MAIC-101)

Mid Term Examination- II  
M. M.: 20  
Time: 9:30 a.m.- 10:20 a.m. (Shift-I)

**NOTE:** Attempt all the Questions. Each Question carries 4 marks.

- Q1. Calculate the approximate value of  $\sqrt{17}$  to four decimal places by taking the first four terms of an appropriate Taylor's series.
- Q2. Show that the rectangular solid of maximum volume that can be inscribed in a sphere is a cube.
- Q3. If  $u = 2xy$ ,  $v = x^2 - y^2$ ,  $x = r\cos\theta$ ,  $y = r\sin\theta$ , evaluate  $\frac{\partial(u,v)}{\partial(r,\theta)}$ .
- Q4. Solve  $\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 29y = 0$ , given that, when  $x = 0$ ,  $y = 0$  and  $\frac{dy}{dx} = 15$ .
- Q5. Solve  $(D^4 + 2D^2 + 1)y = x^2 \cos x$ .
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