## NATIONAL INSTITUTE OF TECHNOLOGY, KURUKSHETRA THEORY EXAMINATION

Question Paper

	Roll No.	
	th and Year of Examination : DEC. 2022	
	ramme : B.Tech Semester: 3 <sup>rd</sup>	
	ect: Field and Waves	
	rse No: ECPC-31 Maximum Marks: 50	
	Number of Questions to be Attempted: 5 Time Allowed: 3 Hrs.	
	Il No. of Questions: 6 Total No. of Pages Used: 3	
	ess stated otherwise, the Symbols have their usual meanings in context with the	ne
	ect. Assume suitably and state, additional data required, if any.	
	Candidates, before starting to write the solutions, should please check the	
	stion Paper for any discrepancy, and also ensure that they have been delivered the	he
ques	stion paper of right course no. and right subject title.	
	Notes Attained and Government All and the second	
1	Note: Attempt any five questions. All questions carry equal marks.	
	The same of the sa	
1a.	Given $\mathbf{F} = \mathbf{a}_x xy - \mathbf{a}_y 2x$ , evaluate the scalar line integral $\int_{\mathbf{F}}^{\infty} \mathbf{F} \cdot d\mathbf{l}$ along the	
	The state of the s	
	quarter circle shown in Fig. 1 using Cartesian and Cylindrical coordinate	
	systems. Comment.	
- 1	<u>``</u> t_	
	Fig. 1	
		2
	d → x	2
1b.	Two infinitely long coaxial cylindrical surfaces, $r = a$ and $r = b$ $(b > a)$ ,	
	carry surface charge densities $\rho_{so}$ and $\rho_{sb}$ , respectively.	
1	i. Determine E everywhere.	
- (	ii. What must be the relation between $a$ and $b$ in order that $E$ vanishes	
	for $r > b$	3
1c.	Determine the E field both inside and outside a spherical cloud of electrons	3
	with a uniform volume charge density $\rho = -\rho_0$ (where $\rho_0$ is a positive	
	quantity) for $0 \le P \le h$ and $a = 0$ for $P > h$ by action $P_0$ is a positive	
	quantity) for $0 \le R \le b$ and $\rho = 0$ for $R > b$ by solving Poisson's and	-
20	Laplace's equation for V.	5
2a.	Determine the capacitance per unit length of a two wire transmission line	
	with parallel conducting cylinders of different radii $a_1$ and $a_2$ , their axes	
	being separated by a distance $D$ (where $D > a_1 + a_2$ ).	3
2b.	Derive equation of continuity for electric charge. Explain its significance	3
	and consequences with the help of a suitable example.	3
2c.	A very long thin conducting strip of width whiles in the xz-plane between	

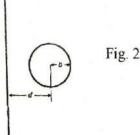
 $x = \pm w/2$ . A surface current  $J_1 = a_1 J_{10}$  flows in the strip. Find the

magnetic flux density at an arbitrary point outside the strip.

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- 3a. A conducting circular loop of a radius 0.1m is situated in the neighborhood of a very long power line carrying a 60-Hz current as shown in Fig. 2 with d = 0.15m. An ac millimeter inserted in the loop reads 0.3mA. Assume the total impedance of the loop including the milliammeter to be  $0.01\Omega$ .
  - i. Find the magnitude of the current in the power line
  - To what angle about the horizontal axis should the circular loop be rotated in order to reduce the milliammeter reading to 0.2mA.



- 3b. Describe briefly Faraday disk generator and the principle behind its working. Draw its neat labeled sketch and derive the expression for generated emf.
- 4a. Derive the general wave equations for E and H in a non conducting simple medium where a charge distribution  $\rho$  and a current distribution J exist. Convert the wave equations to Helmholtz's equations for sinusoidal time dependence. Write the general solutions for E(R,t) and H(R,t) in terms of  $\rho$  and J.
- 4b. It is known that  $\mathbf{E}$  and  $\mathbf{B}$  can be determined from the potentials V and  $\mathbf{A}$ . The vector potential  $\mathbf{A}$  was introduced through the relation  $\mathbf{B} = \nabla \times \mathbf{A}$  because of the solenoidal nature of  $\mathbf{B}$ . In a source free region,  $\nabla \cdot \mathbf{E} = 0$ , we can define another type of vector potential  $\mathbf{A}_e$ , such that  $\mathbf{E} = \nabla \times \mathbf{A}_e$ . Assuming harmonic time dependence
  - i. Express H in terms of  $A_e$
  - ii. Show that A<sub>e</sub> is a solution of a homogeneous Helmholtz's equation.
- 5a. For a harmonic, uniform plane wave propagating in a simple medium, both E and H vary in accordance with the factor e<sup>-/k-R</sup>. Show that the four Maxwell's equations for uniform plane wave in a source-free region reduce to the following:
  - i.  $\mathbf{k} \times \mathbf{E} = \omega \mu \mathbf{H}$
  - ii.  $\mathbf{k} \times \mathbf{H} = -\omega \varepsilon \mathbf{E}$
  - iii.  $\mathbf{k} \cdot \mathbf{E} = 0$
  - iv.  $\mathbf{k} \cdot \mathbf{H} = 0$
- 5b. State and prove Poynting theorem. Explain its significance with the help of a suitable numerical example.
- Show that a plane wave with an instantaneous expression for the electric field  $\mathbf{E}(z,t) = \mathbf{a}_x E_{10} \sin(\omega t kz) + \mathbf{a}_y E_{20} \sin(\omega t kz + \psi)$  is elliptically polarized. Find the polarization ellipse.

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5	b.	A uniform plane wave of angular frequency $\omega$ in medium 1 having a refractive index $n_1$ is incident on a plane interface at $z=0$ with medium 2 having a refractive index $n_2$ ( $< n_1$ ) at the critical angle. Let $E_{10}$ and $E_{10}$ denote the amplitudes of the incident and refracted electric filed intensities, respectively.  i. Find the ratio $E_{10} / E_{10}$ for perpendicular polarization.	
		Find the ratio $E_{in}/E_{in}$ for parallel polarization	
		Write the instantaneous expressions of $E_i(x,z;t)$ and $E_i(x,z;t)$ for	
		perpendicular polarization in terms of the parameters $\omega$ , $n_1$ , $n_2$ , $\theta_i$ and $E_{i0}$ .	6
	6a. 6b.	Demonstrate mathematically that the field quantities in free space manifest themselves as circuit quantities when bounded by infinite parallel conductors.  Derive TE mode field expressions in a rectangular waveguide. Also give expressions for cut-off frequency and corresponding wavelength. Explain which	5
		mode is the dominant mode and reason thereof.	5
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	6a.	The characteristic impedance of a given lossless transmission line is 75 $\Omega$ . Use a Smith chart to find the input impedance at 200 MHz of such a line that is	
		l	
		:: 0.9 m long and short circuited	5
		· danadana input admillances also.	
	6b.	Write a short note on cavity resonator and explain its practical significance with	5
		the help of an example.	