

Date:07-05-2024

NATIONAL INSTITUTE OF TECHNOLOGY, KURUKSHETRA (An Institution of National Importance under Ministry of Education, Govt. of India) DEPARTMENT OF MATHEMATICS

END SEMESTER EXAMINATIONS, MAY 2024

B. TECH IV Sem. (ECE -A &B)

MAIC-204: Applied Linear Algebra (Maths-III)

Time: 09:30 AM to 12:30 PM

Max. Marks: 50

N.B.: Answer ALL questions.

Answers to all parts of each question should be in one place.

	This wors to air parts of each queen
Q1 I	Let $V \equiv \text{Set of all polynomials of degree } n \text{ over real field } \mathbb{R}$, $W \equiv \text{Set of all polynomials of } \mathbb{R}$.
	degree of a over real field ID and 7 = Set of all polynomials over real field ID
	Dravia (Diameter that U(D) M(D) and 7(R) are vector space over In. If any structure
LAMBOUR & SE	the discount has basis and dimension
/	vector space, then discuss their basis and dimension. Find the range space $R(T)$ and null space $N(T)$ for the given linear operator. Also, find the basis and
Q2,	Find the range space $R(T)$ and null space $R(T)$ and $R(T)$
/	Find the range space $R(T)$ and null space $N(T)$ for the graph $T: \mathbb{R}^3(\mathbb{R}) \to \mathbb{R}^3(\mathbb{R})$ such that $T(x,y,z) = (x+y,y+z,x-z)$. Also, find the basis and [6M]
1	dimensions of $R(T)$ and $N(T)$.
Q3	dimensions of $R(T)$ and $N(T)$. \checkmark Find the annihilator space W^0 for the sub space W of $\mathbb{R}^3(\mathbb{R})$ spanned by (1,2,0), (1,0,5) and [6M]
	(U, -2,5). Also, show that atm (W) + atm (W)
QA	Find the eigen values and eigen vectors for the given linear operator $T^{100} + 5T^{20} + 20I$ and such that $T(x,y) = (y,x)$. Also evaluate i) $ T^{100} + 5T^{20} + 20I $ [6M]
/	such that $T(x,y) = (y,x)$. Also evaluate i) $I^{T} = I^{T}$ [6M]
	ii) $Trace(T^{100} + 5T^{20} + 20I)$.
05	ii) $Trace(T^{100} + 5T^{20} + 20I)$. Find the characteristic and minimal polynomial for the given linear operator $T(x,y,z) = (5x - 6y - 6z, -x + 4y + 2z, 3x - 6y - 4z)$
Q5	Find the characteristic and minimal polynomial for the given $T: \mathbb{R}^3(\mathbb{R}) \to \mathbb{R}^3(\mathbb{R})$ such that $T(x,y,z) = (5x - 6y - 6z, -x + 4y + 2z, 3x - 6y - 4z)$ [6M]
	Also, discuss the diagonalization of T^{100} .
06	Also, discuss the diagonalization of T^{100} . Define inner product space. Give an example of an inner product space with proper product space with proper space. Show that for the given linear operator T^{100} .
Q6	Define inner product space. Give an example of an inner product space linear operator explanation. Define invariant sub-space. Show that for the given linear operator explanation. Define invariant sub-space. Show that for the given linear operator T_1 and T_2 and T_3 are invariant under T_2 .
	explanation. Define invariant sub-space. Show that To the gradual sub-space $T: \mathbb{R}^3(\mathbb{R}) \to \mathbb{R}^3(\mathbb{R})$, if T_1 is any polynomial in T then $R(T_1)$ and $N(T_1)$ are invariant under $T: \mathbb{R}^3(\mathbb{R}) \to \mathbb{R}^3(\mathbb{R})$, if T_1 is any polynomial in T then T
	T
Q7	T. Apply Gram-Schmidt Process on {(3,0,4), (-1,0,7), (2,9,11)} to obtain an orthogonal basis [6M]
Q8	TIME FINDS (W) CIVEN DV
1	Consider the sub-spaces W_1 and W_2 of \mathbb{R} (\mathbb{R}) given by $W_1 = \{(x, y, z) x + y + z = 0\}$, $W_2 = \{(x, y, z) x - y + z = 0\}$. If W is a sub-space of $W_1 = \{(x, y, z) x + y + z = 0\}$.
	$\mathbb{R}^3(\mathbb{R})$ such that
100	2 ((0.1.1))
10000	a) $W \cap W_2 = Span\{(0,1,1)\}$ b) $W \cap W_1$ is orthogonal to $W \cap W_2$ with respect to usual dot product (inner product
	$\mathbb{R}^3(\mathbb{R})$.
1/2	Then which of the followings are true?
	1 ((A 1 -1) (() 1 1 1)
1 5 6	1 (10 1) (01 -1)
No.	0 ((10 1) (101))
	$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty$
E II. O.	$(v) \dim(W_1) = 1$ $(vi) \dim(W_2) = 2$ $(6M)$